

INTEGRATED UNIT 2: GEOMETRY IN THE ALHAMBRA

MOSAICS IN THE NASRID PALACE





Let's begin the unit watching the video.

"La Alhambra y las matemáticas"

Let's begin the unit watching the video.

"La Alhambra y las matemáticas"

Let's see some examples of mosaics you can find in the Alhambra

















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You will create your own mosaic!

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Now you know a few things about the relationship between the Alhambra and maths, but you need more information to be ready for this unit.

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1) ¿Por qué los árabes usaban tanto la geometría para las decoraciones de sus palacios?

2) ¿Cuál es el número áureo o de oro? ¿Por qué es tan importante?

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1) ¿Por qué los árabes usaban tanto la geometría para las decoraciones de sus palacios?

2) ¿Cuál es el número áureo o de oro? ¿Por qué es tan importante?

3) ¿Qué es un rectángulo áureo? ¿En qué lugar de la Alhambra podemos encontrar rectángulos áureos?

- El informe debe cumplir las siguientes características.
- Los formatos aceptados son: documento de texto (2 páginas como máximo) o presentación.
- Debe tener un título (piensa en uno original).
- Tamaño de letra 12.
- Las respuestas deben ir acompañadas por imágenes, dibujos o gráficos.
- Redacta tus respuestas, el simple "corta-pega" será penalizado.

TASK 2. WHAT IS A TESSELLATION?

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Here you are an example.









♦ Each piece of this drawing is a TILE.



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For practical reasons, for example, when you have to cover the ground with paving stone, it is easier and cheaper to get all the tiles having the same shape.



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- For practical reasons, for example, when you have to cover the ground with paving stone, it is easier and cheaper to get all the tiles having the same shape.
- When you cover a surface with a pattern of tiles with no gaps or overlaps, this is called a TESSELLATION or TILING.





You can make tessellations by using ...



You can make tessellations by using ...

squares,





You can make tessellations by using ...

squares, equilateral triangles







You can make tessellations by using ...

squares, equilateral triangles and hexagons.















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- There is no need to use any measuring tool to get that.


- Activity 2. Is it possible to cover a surface with other regular polygons?

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 - There is no need to use any measuring tool to get that.
- ♦ Just use maths and the following rule.

"the interior angles of a triangle add up to 180° ".



- Activity 2. Is it possible to cover a surface with other regular polygons?

- To answer that question you have to measure the interior angles of a regular polygon.
 - There is no need to use any measuring tool to get that.
- ♦ Just use maths and the following rule.
 - "the interior angles of a triangle add up to 180°".
 - Besides, you can divide a polygon into triangles so, for example, to work out the interior angles of a square...



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= **180°** + **180°** = **360°**



Besides, you can divide a polygon into triangles so, for example, to work out the interior angles of a square...



 $+ + + + + + + = = = 180^{\circ} + 180^{\circ} = 360^{\circ}$ $= \frac{360^{\circ}}{4} = 90^{\circ}$





Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	\bigtriangleup	180°	60°
Square				
		\bigcirc		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	$ \bigcirc$	180°	60°
Square	4			
		\bigcirc		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	\bigtriangleup	180°	60°
Square	4		2·180° = 360°	
		\bigcirc		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	\bigtriangleup	180°	60°
Square	4		2·180° = 360°	360°/4 = 90°
		\bigcirc		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	$ \bigcirc$	180°	60°
Square	4		2·180° = 360°	$360^{\circ}/4 = 90^{\circ}$
Pentagon		\bigcirc		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	$ \bigcirc$	180°	60°
Square	4		2·180° = 360°	360°/4 = 90°
Pentagon	5	\bigcirc		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	$ \bigcirc$	180°	60°
Square	4		2·180° = 360°	$360^{\circ}/4 = 90^{\circ}$
Pentagon	5	\bigcirc		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	$ \bigcirc$	180°	60°
Square	4		2·180° = 360°	360°/4 = 90°
Pentagon	5	$\widehat{\Box}$	3·180° = 540°	



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Triangle	3	\sum	180°	60°
Square	4		2·180° = 360°	$360^{\circ}/4 = 90^{\circ}$
Pentagon	5	$\widehat{\Box}$	$3.180^{\circ} = 540^{\circ}$	540°/5 = 108°



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon		\bigcirc		
Octagon		\bigcirc		
•••	• • •			
Any Polygon	n	(n)		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	\bigcirc		
Octagon		\bigcirc		
•••	• • •	•••	••••	•••
Any Polygon	n	(\mathbf{n})		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	\bigcirc		
Octagon		\bigcirc		
•••	• • •	•••	•••	•••
Any Polygon	n	(n)		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	\bigcirc	4·180 = 720°	
Octagon		\bigcirc		
•••	• • •	•••	••••	•••
Any Polygon	n	(\mathbf{n})		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	\square	4·180 = 720°	720°/6 = 120°
Octagon		\bigcirc		
•••	• • •	•••		
Any Polygon	n	(\mathbf{n})		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	$\langle \rangle$	4·180 = 720°	720°/6 = 120°
Octagon	8	\bigcirc		
•••	• • •		••••	•••
Any Polygon	n	(\mathbf{n})		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	(4·180 = 720°	720°/6 = 120°
Octagon	8	?		
•••	• • •	•••	••••	•••
Any Polygon	n	(\mathbf{n})		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	$\langle \rangle$	4·180 = 720°	720°/6 = 120°
Octagon	8	?	6·180° = 1080°	
• • •	•••	•••	•••	•••
Any Polygon	n	(\mathbf{n})		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	(4·180 = 720°	720°/6 = 120°
Octagon	8	?	6·180° = 1080°	1080°/8 = 135°
• • •	•••	•••	••••	•••
Any Polygon	n	n		



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	$\langle \rangle$	4·180 = 720°	720°/6 = 120°
Octagon	8	?	6·180° = 1080°	1080°/8 = 135°
• • •	• • •	•••	••••	•••
Any Polygon	n	(n)	(n-2)·180°	



Shape	Sides	Break it into triangles	Sum of Interior Angles	Each Angle
Hexagon	6	\bigcirc	4·180 = 720°	720°/6 = 120°
Octagon	8	?	6·180° = 1080°	1080°/8 = 135°
• • •	• • •	•••	•••	•••
Any Polygon	n	(\mathbf{n})	(n-2)·180°	(n-2)·180°/n



So the general rule is.



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Each angle of a regular polygon = $(n-2) \times 180^{\circ} / n$



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So what happen if we get together regular polygons to make a tessellation?





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Each angle of a regular polygon = $(n-2) \times 180^{\circ} / n$

So what happen if we get together regular polygons to make a tessellation?



The addition of the interior angles of the polygons that share one vertex must be 360°.

Then it is impossible to use any other regular polygons but squares, equilateral triangles and hexagons

squares

squares



$$90^{\circ} \cdot 4 = 360^{\circ}$$



$$90^{\circ} \cdot 4 = 360^{\circ}$$
Then it is impossible to use any other regular polygons but squares, equilateral triangles and hexagons because the only ones whose interior angles are divisors of 360° are:



$$90^{\circ} \cdot 4 = 360^{\circ}$$

 $60^\circ \cdot 6 = 360^\circ$

Then it is impossible to use any other regular polygons but squares, equilateral triangles and hexagons because the only ones whose interior angles are divisors of 360° are:



Then it is impossible to use any other regular polygons but squares, equilateral triangles and hexagons because the only ones whose interior angles are divisors of 360° are:





- Activity 3. Geometric transformations

Let's watch this video.

Colin Dodds - Geometric Transformations (Math Song)



- Activity 3. Geometric transformations

Let's watch this video.

Colin Dodds - Geometric Transformations (Math Song)

These are geometric transformations.









ROTATION "turn it 'round"







"bnuor' fi nruf"







ROTATION "turn it 'round"



















TRANSLATION \rightarrow

TRANSLATION "shift it left, right, up, or down"









"shift it left, right, up, or down"

Before translation





"shift it left, right, up, or down"

Before translation Vector of translation



"shift it left, right, up, or down"

Before translation





"copy it across an axis of symmetry"



"copy it across an axis of symmetry"



"copy it across an axis of symmetry"

"copy it across an axis of symmetry"

REFLECTION



"copy it across an axis of symmetry"





"copy it across an axis of symmetry"



Axis of symmetry



"copy it across an axis of symmetry"



Now answer the questions about geometric transformations on the worksheets.
The ancient artisans knew the restriction about the regular polygons and tried to make prettier tessellations by...

The ancient artisans knew the restriction about the regular polygons and tried to make prettier tessellations by...

using different colours

The ancient artisans knew the restriction about the regular polygons and tried to make prettier tessellations by...

> using different colours

> making some distortion to the original tile

The ancient artisans knew the restriction about the regular polygons and tried to make prettier tessellations by...

using different colours

- making some distortion to the original tile
- ♦ repeating it alongside the whole surface

- Activity 1. "El hueso nazarí"

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Take a look at this video to find out how the "hueso nazarí" is constructed and repeat the construction

http://concurso.cnice.mec.es/cnice2006/material105/Mo saicos/hueso.htm

- Activity 1. "El hueso nazarí"

1) Draw the diagonals of the square.



- Activity 1. "El hueso nazarí"

2) Draw two parallel lines to the sides.



- Activity 1. "El hueso nazarí"

3) Remove some lines.



- Activity 1. "El hueso nazarí"

3) Remove some lines.



- Activity 1. "El hueso nazarí"

4) Complete the bone.



- Activity 1. "El hueso nazarí"

Draw the bone using the pattern on your grid and colour it to your own liking.



- Activity 2: "El avión nazarí"

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You can see the construction of the plane in this link.

http://concurso.cnice.mec.es/cnice2006/material105/Mo saicos/avion.htm

– Activity 2. "El avión nazarí"

1) Draw two perpendicular lines



- Activity 2: "El avión nazarí"

2) Draw a segment like this.



– Activity 2. "El avión nazarí"

3) Rotate the triangle 90° clockwise from this centre.



– Activity 2. "El avión nazarí"

3) Rotate the triangle 90° clockwise from this centre.



– Activity 2. "El avión nazarí"

4) Apply a reflection from this axis and complete the plane.



– Activity 2. "El avión nazarí"

4) Apply a reflection from this axis and complete the plane.



– Activity 2. "El avión nazarí"

Draw the plane using the pattern on your grid and colour it to your own liking.



- Activity 3: "La pajarita nazarí"

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For the third tessellation we use a property of an equilateral triangle.

- Activity 3. "La pajarita nazarí"

For the third tessellation we use a property of an equilateral triangle.

It has rotational symmetry by 60°, that is, you can turn an equilateral triangle by 60° and get the same shape.

- Activity 3. "La pajarita nazarí"

If you translate that property to our triangle tessellation.

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If you translate that property to our triangle tessellation.



- Activity 3: "La pajarita nazarí"

If you translate that property to our triangle tessellation.



Any transformation you do to one side of a triangle can be replicated by rotating it 60° and there'll be no gaps.

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If you translate that property to our triangle tessellation.





Any transformation you do to one side of a triangle can be replicated by rotating it 60° and there'll be no gaps.

- Activity 3. "La pajarita nazarí"

Here you can see the construction of the "pajarita".

http://concurso.cnice.mec.es/cnice2006/material105/Mo saicos/pajarita.htm