UNIT 7. SYSTEMS OF EQUATIONS

(3º ESO)

HISTORY

Mathematicians inf Babylon studied both equations and system of equations. However, they were much more interested in the latter. They devised and solve linear systems of equations with several unknowns. They called these unknowns *length*, *width*, *volume*, *area...* even if they had nothing to do with geometry.

In Babylon, they solved problems using guesswork. They tried different amounts until they got the right solution. The following problem appears on one of their tablets:

 $\frac{1}{4} width + length = 7 hands$ width + length = 10 feet

Diophantus devised algebraic problems that could easily be made into systems of equations. He solved them by carefully choosing and naming an unknown that allowed him to create one single equation.

SYSTEMS OF LINEAR EQUATIONS

Two equations form a system of equations when we work with them to find their common solution.

When two equations form a system, we write them like this:

$$ax + by = c$$
$$a'x + b'y = c'$$

The **solution** to a system is the common solution to both equations.

VOCABULARY & EXPRESSIONS

- \Rightarrow **Equation**: Ecuación
- ⇒ System of equations: sistema de ecuaciones
- \Rightarrow **Coefficient**: coeficiente
- \Rightarrow **Unknowns**: incógnitas
- ⇒ Independent term: término independiente

 \Rightarrow **Degree**: grado

 \Rightarrow **Solve**: resolver

- \Rightarrow **Solution**: solución
- ⇒ Inconsistent system: Sistema incompatible
- ⇒ Independent system: sistema compatible determinado
- ⇒ Dependent system: Sistema compatible indeterminado
 - ⇒ Elimination method: método de reducción
 - ⇒ Equalisation method: método de igualación
 - ⇒ Substitution method: método de sustitución

NUMBER OF SOLUTIONS OF A SYSTEM OF LINEAR EQUATIONS

The number of solutions of a system of linear equations is:

- Zero solutions. The graphic representation of this is two parallel straight lines. This system is called inconsistent system.
- **One solution**. The graphic representation of this is two straight lines that intersect at a single point. This system is called **independent system**.
- Infinite solutions. The graphic representation of this is two coincident straight lines. This system is called **dependent system**.



Infinite solutions



